## 台北醫學大學微積分第一次平時測驗命題紙

系級	授課教師	考試日期	學號	· 姓名
醫學系	潘力誠			

- 1. Let  $\vec{F} = (1, 2, 3)$ , and let  $\rho$  be the plane x + y + z = 3. Find the component of  $\vec{F}$  normal to  $\rho$  and the projection of  $\vec{F}$  normal to  $\rho$ . (10%)
- 2. Find the nth order Taylor polynomial for cos (x). (10%)
- 3. Compute the derivative of function  $f(x) = \frac{(x^2 + 2x + 3 \sqrt{2})\tan x}{x^2 \pi x}$ . (10%)
- 4. Find the extrema of  $f(x) = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$ . (10%)
- 5. Find the slope of a logistic function  $f(t) = \frac{1.25}{1+1.25e^{-0.4t}}$  at t=10 (10%)
- 6. Three ropes of lengths, R1, R2, and R3 are suspended from the ceiling at positions  $\vec{A}$ ,  $\vec{B}$ , and  $\vec{C}$  as in the figure. The other ends are tied to a weight at  $\vec{P}$  that pulls the ropes tight. Find the coordinate of  $\vec{P}$  given that R1=2, R2=1.5, R3=1.5,  $\vec{A}$ =(1,0,0),  $\vec{B}$ =(0,1,0), and  $\vec{C}$ =(1,1,0). (10%)
- 7. Approximate the root of  $y = x^3 + 3x^2 5$ , using Newton's method and  $c_0 = 1$  as initial guess. (10%)
- 8. Sketch the trace of vector  $\vec{r} = \vec{r}1 + \vec{r}2$ , where  $\vec{r}1 = (2t + 1, -2t)$  and  $\vec{r}2 = (\cos(2\pi t), \sin(2\pi t))$ . (10%)
- 9. Find the equation of the normal line to the graph of  $f(x) = \ln(x(x^2 + 1)^2)$ , at x = 5. (10%)

10. Find the least square line for the given data. (10%)

X	у	
10	84	
20	71	
30	80	
40	73	
50	60	
60	52	
70	56	
80	46	
90	36	